

Дано: l, M, G, J_k, W_k

Найти: $M_{кр}, \tau_{max}, \varphi, A$ и U .

$$\sum M_z = 0 = -M_{RB} - M$$

$$M_{RB} = -M$$

$$\sum M_{y_1} = 0 = M + M_{KP1}$$

$$M_{KP1} = -M$$

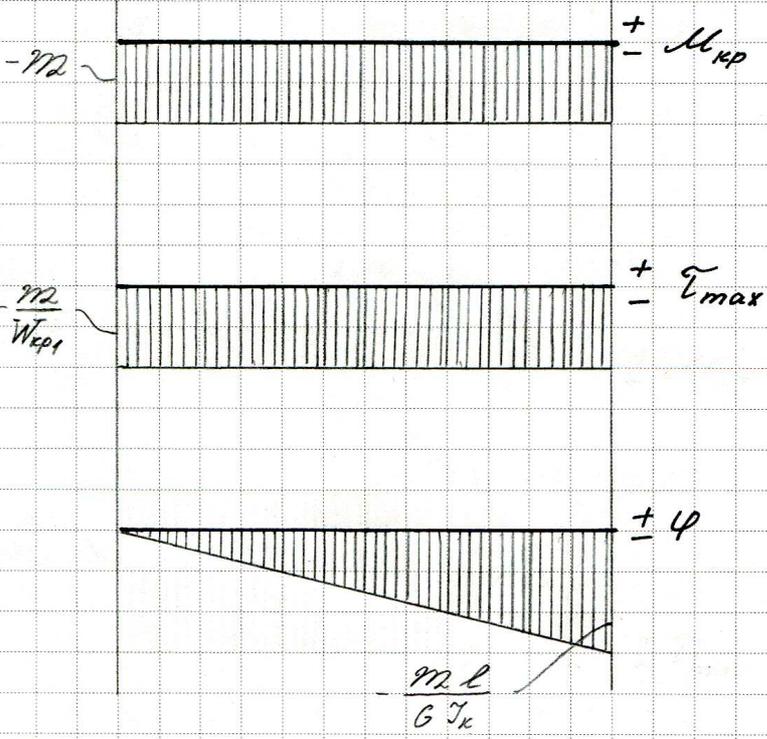
$$\tau_{max,1} = \frac{M_{KP1}}{W_{k1}} = -\frac{M}{W_{k1}}$$

$$\varphi_1 = \varphi_0^{кон} + \int_0^{z_1} \frac{M_{KP1} dz_1}{G_1 J_{k1}} =$$

$$= - \int_0^{z_1} \frac{M \cdot dz_1}{G J_k} = -\frac{M \cdot z_1}{G \cdot J_k}$$

$$z_1 = 0: \varphi_1^{кон} = 0$$

$$z_1 = l: \varphi_1^{кон} = -\frac{M \cdot l}{G \cdot J_k}$$



Работа внешних моментов:

$$A = \sum_i^1 M_i \varphi_i = \frac{1}{2} M_B \cdot \varphi_B + \frac{1}{2} M_C \cdot \varphi_C =$$

$$= \frac{1}{2} M \cdot 0 + \frac{1}{2} (-M) \cdot \left(-\frac{M \cdot l}{G J_k}\right) = \frac{M^2 l}{2 G J_k}$$

Потенциальная энергия деформации:

$$U = \sum_i \frac{M_{кр i}^2 \cdot l_i}{2 G_i J_{k i}} = \frac{M_{кр 1}^2 \cdot l_1}{2 G_1 J_{k 1}} = \frac{(-M)^2 \cdot l}{2 G J_k} = \frac{M^2 l}{2 G J_k}$$

$$A = U$$